## Cambridge Assessment International Education

Cambridge International General Certificate of Secondary Education

## MATHEMATICS <br> 0580/41

Paper 4 (Extended)
October/November 2018
MARK SCHEME
Maximum Mark: 130

## Published

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

Cambridge International will not enter into discussions about these mark schemes.
Cambridge International is publishing the mark schemes for the October/November 2018 series for most Cambridge IGCSE ${ }^{\text {TM }}$, Cambridge International A and AS Level components and some Cambridge O Level components.

## Generic Marking Principles

These general marking principles must be applied by all examiners when marking candidate answers. They should be applied alongside the specific content of the mark scheme or generic level descriptors for a question. Each question paper and mark scheme will also comply with these marking principles.

## GENERIC MARKING PRINCIPLE 1:

Marks must be awarded in line with:

- the specific content of the mark scheme or the generic level descriptors for the question
- the specific skills defined in the mark scheme or in the generic level descriptors for the question
- the standard of response required by a candidate as exemplified by the standardisation scripts.

GENERIC MARKING PRINCIPLE 2:
Marks awarded are always whole marks (not half marks, or other fractions).

## GENERIC MARKING PRINCIPLE 3:

Marks must be awarded positively:

- marks are awarded for correct/valid answers, as defined in the mark scheme. However, credit is given for valid answers which go beyond the scope of the syllabus and mark scheme, referring to your Team Leader as appropriate
- marks are awarded when candidates clearly demonstrate what they know and can do
- marks are not deducted for errors
- marks are not deducted for omissions
- answers should only be judged on the quality of spelling, punctuation and grammar when these features are specifically assessed by the question as indicated by the mark scheme. The meaning, however, should be unambiguous.

GENERIC MARKING PRINCIPLE 4:
Rules must be applied consistently e.g. in situations where candidates have not followed instructions or in the application of generic level descriptors.

## GENERIC MARKING PRINCIPLE 5:

Marks should be awarded using the full range of marks defined in the mark scheme for the question (however; the use of the full mark range may be limited according to the quality of the candidate responses seen).

GENERIC MARKING PRINCIPLE 6:
Marks awarded are based solely on the requirements as defined in the mark scheme. Marks should not be awarded with grade thresholds or grade descriptors in mind.

## Abbreviations

| cao | correct answer only |
| :--- | :--- |
| dep | dependent |
| FT | follow through after error |
| isw | ignore subsequent working |
| oe | or equivalent |
| SC | Special Case |
| nfww | not from wrong working |
| soi | seen or implied |


| Question | Answer | Marks | Partial Marks |
| :---: | :---: | :---: | :---: |
| 1(a)(i) | 2.25 final answer | 2 | M1 for $\frac{3}{5+3}$ or $\frac{6}{5+3}$ oe |
| 1(a)(ii) | 37.5 | 1 | $\text { FT their } \frac{(\mathbf{a})(\mathbf{i})}{6} \times 100$ |
| 1(a)(iii) | $5.5[0]$ or 5.499 to 5.500 | 2 | M1 for $6 \div 1.091$ |
| 1(b) | 21 | 3 | M2 for $15 \times \sqrt{\frac{352.8}{15 \times 12}}$ oe or SC2 for answer 16.8 or M1 for $\sqrt{\frac{352.8}{15 \times 12}}$ or $\sqrt{\frac{15 \times 12}{352.8}}$ seen or M1 for a correct implicit statement for the length |
| 1(c) | 525 | 3 | M2 for $\frac{483}{100-8}[\times 100]$ oe or M1 for 483 associated with 92 [\%] |
| 2(a)(i) | Translation $\binom{5}{8}$ | 2 | B1 for each <br> Accept 5 right and 8 up |
| 2(a)(ii) | Enlargement [sf] 0.5 oe [centre] $(0,-7)$ | 3 | B1 for each |
| 2(a)(iii) | Rotation <br> 90 [anticlockwise] oe Origin oe | 3 | B1 for each |
| 2(b) | $\begin{aligned} & \text { Image at }(-8,1)(-8,5)(-8,7) \\ & (-4,1) \end{aligned}$ | 2 | B1 for reflection of flag $A$ in the line $x=-1$ <br> or $y=k$ or for vertices of triangle in correct place but not joined |


| Question | Answer | Marks | Partial Marks |
| :---: | :---: | :---: | :---: |
| 3(a) | $\begin{array}{llll}0 & -2 & 0.9\end{array}$ | 3 | B1 for each |
| 3(b) |  | 4 | B3 FT for 9 or 10 points or B2 FT for 7 or 8 points or B1 FT for 5 or 6 points |
| 3(c) | $\begin{aligned} & \hline-0.45 \text { to }-0.35 \\ & 1 \\ & 2.35 \text { to } 2.45 \end{aligned}$ | 3 | FT their graph <br> B1 for each in the correct position If zero scored, SC1FT for 3 correct values |
| 3(d)(i) | $y=1-x$ oe | 2 | B1 for $y=1-k x$ oe, $k \neq 0$ or $y=k-x$ oe or $1-x$ |
| 3(d)(ii) | Correct ruled line and 2.25 to 2.4 | 3 | B2FTdep for correct ruled line <br> or B1 dep for line through $(0,1)$ when extended but not $y=1$ or with gradient -1.1 to -0.9 or correct line but freehand or SC2 for $y=x-1$ ruled after answer $[y=] x-1$ in (d)(i) <br> and <br> B1 for 2.25 to 2.4 |
| 3(e) | Correct tangent and 1.7 to 3.7 | 3 | No daylight between tangent and curve at $x=-0.25$. Point of contact is the midpoint between two vertices of daylight and this point of contact must be between -0.35 and -0.15 <br> B2 for close attempt at tangent at $x=-0.25$ and answer in range OR <br> B1 for ruled tangent at $x=-0.25$, no daylight <br> Consider point of contact as midpoint between two vertices of daylight, the midpoint must be between $x=-0.35$ and $-0.15$ <br> and M1 dep on B1 or close attempt at tangent at $x=-0.25$ for $\frac{\text { rise }}{\text { run }}$ |
| 4(a) | 100.2 nfww | 4 | M1 for midpoints soi 65, 80, 95, 105, $112.5,120$ <br> M1 for use of $\sum f x$ with $x$ in correct interval including both boundaries <br> M1dep for $\sum f x \div 180$ dep on previous M1 |
| 4(b) | $\begin{aligned} & 0.8 \\ & 2.8 \\ & 0.65 \end{aligned}$ | 3 | B1 for each <br> If zero scored, SC1 for 1.6, 5.6 and 1.3 seen |


| Question | Answer | Marks | Partial Marks |
| :---: | :---: | :---: | :---: |
| 4(c) | $\begin{array}{lllll}8 & 34 & 69 & 136 & 164\end{array}$ | 2 | B1 for one error $\mathbf{F T}$ other values or for 3 or 4 correct |
| 4(d) | Correct diagram | 3 | B1FT for correct vertical placement for 6 plots <br> B1 for correct horizontal placement for 6 plots <br> B1FT dep on at least B1 for reasonable increasing curve or polygon through their 6 points If zero scored, SC1FT for 5 out of 6 correct plots |
| 4(e)(i) | 15 to 17 | 2 | $\begin{aligned} & \text { B1 for }[\mathrm{LQ}=] 93 \text { to } 94 \text { or }[\mathrm{UQ}=] 109 \text { to } \\ & 110 \end{aligned}$ |
| 4(e)(ii) | 107 to 109 | 2 | B1 for 126 seen |
| 4(e)(iii) | 66 to 72 | 2 | FT their graph for 2 marks B1 for answer 106 to 114 or B1FT their graph reading at 106 cm seen |
| 5(a)(i) | $\begin{aligned} & {[h=] 253.8 \div 18 \div\left(\frac{6}{2}\right) \text { or }} \\ & {[h=] \frac{253.8 \times 2}{6 \times 18} \text { or }} \\ & {[h=] \frac{253.8}{18 \times \frac{6}{2}}} \end{aligned}$ | 3 | For M3 no errors at any stage M2 for $253.8=\frac{1}{2} \times 6 \times h \times 18$ oe (no previous errors) or M1 for triangle area $=\frac{1}{2} \times 6 \times h$ soi |
| 5(a)(ii) | 38.1 or 38.06 to 38.08 | 2 | M1 for $\tan =\frac{4.7}{6}$ oe |
| 5(b) | 358 or 357.9 to 358 | 6 | M1 for $6^{2}+4.7^{2}$ <br> M1 for $\sqrt{6^{2}+4.7^{2}} \times 18[\times 2]$ <br> M1 for $6 \times 18[\times 2]$ <br> M1 for $4.7 \times 18$ <br> M1 for $2 \times \frac{1}{2} \times 6 \times 4.7$ oe |
| 6(a)(i) | 14 | 1 |  |
| 6(a)(ii) | 16 | 1 |  |
| 6(a)(iii) | $\frac{20}{462} \mathrm{oe}$ | 3 | $\begin{aligned} & \text { M2 for } \frac{5}{22} \times \frac{4}{21} \\ & \text { or M1 for } \frac{5}{22} \text { seen } \end{aligned}$ |


| Question | Answer | Marks | Partial Marks |
| :---: | :--- | ---: | :--- |
| 6(a)(iv) | Correct shading |  | $\mathbf{1}$ |
|  |  |  |  |


| Question | Answer | Marks | Partial Marks |
| :---: | :---: | :---: | :---: |
| 8(c) | $y=-\frac{4}{5} x-2 \text { oe }$ | 2 | FT their gradient from $\mathbf{8 ( b )}$ <br> B1 for $y=($ their gradient $) x+c(c \operatorname{not} 0)$ or for $y=m x-2(m \neq 0)$ <br> or for $-\frac{4}{5} x-2$ alone |
| 8(d)(i) | $y=\frac{5}{4} x+4 \text { oe }$ | 3 | M1 for $-\frac{1}{\text { their } \text { gradient }}$ from $\mathbf{8 ( b )}$ M1 for $(8,14)$ substituted into their $y=m x+c$ or $\frac{y-14}{x-8}=m$ or better |
| 8(d)(ii) | 8.54 or 8.544... | 3 | M2 for $(14-\text { their } 6)^{2}+(8-\text { their } 5)^{2}$ or better <br> or M1 for 14 -their 6 and 8 -their 5 seen |
| 8(d)(iii) | $(4,6)$ | 2 | B1 for each |
| 9(a)(i) | $\frac{72}{m}$ | 1 |  |
| 9(a)(ii) | $\frac{72}{m+0.9}$ | 1 |  |
| 9 (b) | $\frac{72}{m}-\frac{72}{m+0.9}=4 \mathrm{oe}$ | M1 | FT their (a)(i) and (a)(ii) if expressions in $m$ |
|  | $72(m+0.9)-72 m=4 m(m+0.9)$ oe | M1 | Dependent on M1 and correct fractions |
|  | $[72 m-72 m]+64.8=4 m^{2}+3.6 m$ oe nfww | A1 |  |
|  | Correct completion to $10 m^{2}+9 m-162=0$ | A1 |  |
| 9 (c)(i) | 3.6 and -4.5 final answer | 3 | B2 for $(2 m+9)(5 m-18)$ or <br> $\frac{-9 \pm \sqrt{(9)^{2}-4(10)(-162)}}{2 \times 10}$ or better <br> or $\mathbf{B 1}$ for $(a m+b)(c m+d)$ where ac $=10$ <br> and either $b d=-162$ <br> or $a d+b c=9$ <br> or for $\sqrt{(9)^{2}-4(10)(-162)}$ or better or $\frac{-9 \pm \sqrt{q}}{2(10)}$ or better |
| 9(c)(ii) | 20 | 1 |  |


| Question | Answer | Marks | Partial Marks |
| :---: | :---: | :---: | :---: |
| 10(a) | 132.26 to 132.28 or 132.3 | 5 | B1 for angle $A B O$ or angle $C B O=90$ soi <br> M1 for $\tan [X O B]=\frac{15}{8}$ oe <br> M1 for $\tan [B O Y]=\frac{22.4}{8}$ oe <br> A1 for $[B O Y=] 70.3 \ldots$ or $[X O B=] 61.9 \ldots$. |
| 10(b) | 18.4 or 18.5 or 18.43 to 18.48 | 2 | M1 for $\frac{\text { their } \mathbf{( a )}}{360} \times 2 \times \pi \times 8$ oe |
| 10(c) | 75.7 to 75.9 | 4 | M1 for $\frac{1}{2}(15+22.4) \times 8$ oe M2 for $\frac{\text { their }(\mathbf{a})}{360} \times \pi \times 8^{2}$ oe or M1 for one sector either $\frac{i n v \tan \left(\frac{15}{8}\right)}{360} \times \pi \times 8^{2} \mathrm{oe}$ $\text { or } \frac{i n v \tan \left(\frac{22.4}{8}\right)}{360} \times \pi \times 8^{2} \text { oe }$ |
| 11(a) | $5\left(m-2 p^{2}\right)\left(m+2 p^{2}\right)$ final answer | 3 | M2 for $(5 m+k)(m+j)$ where $k j=-20 p^{4}$ or $5 j+k=0$ or M1 for $5\left(m^{2}-4 p^{4}\right)$ seen |
| 11(b) | $[P=] \frac{100 \mathrm{~A}}{100+T R}$ final answer | 3 | M1 for $100 A=100 P+P R T$ or for $A=P\left(1+\frac{R T}{100}\right)$ <br> M1 for $100 A=P(100+R T)$ or for $\frac{A}{1+\frac{R T}{100}}=P$ <br> or for $100 A=P(1+R T)$ after $100 A=P+P R T$ as first step |

